# ESTIMATION OF RECURSIVE ORDER NUMBER OF PHOTOCOPIED DOCUMENT BASED ON PROBABILITY DISTRIBUTIONS

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# **ABSTRACT**

Photocopy documents are very common in our normal life. People are permitted to carry and present photocopied documents to avoid damages to the original documents. But this provision is misused for temporary benefits by fabricating fake photocopied documents. Fabrication of fake photocopied document is possible only in 2<sup>nd</sup> and higher order recursive order of photocopies. Whenever a photocopied document is submitted, it may be required to check its originality. When the document is 1<sup>st</sup> order photocopy, chances of fabrication may be ignored. On the other hand when the photocopy order is 2<sup>nd</sup> or above, probability of fabrication may be suspected. Hence when a photocopied document is presented, the recursive order number of photocopy is to be estimated to ascertain the originality. This requirement demands to investigate methods to estimate order number of photocopy. In this work, a different approach based on probability distributions like normal, extreme values and exponential is proposed to estimate the recursive order number of the photocopied document under consideration. A detailed experimentation is performed on a generated data set and the method exhibits efficiency close to 84%.

## **KEYWORDS**

fabricated photocopy documents, recursive order number, probability distributions

# 1. Introduction

Many authorities trust and accept the photocopied documents submitted by citizens as proof and consider the same as genuine. Few such applications like to open bank account, applying for gas connection, requesting for mobile sim card, concerned authorities insist photocopy documents like voter id, driving license, ration card, pan card and passport as proof of address, age, photo id etc to be submitted along with the application form. Certain class of people could exploit the trust of the authorities, and indulge in forging/ tampering/ fabricating photocopy document. These things would be deliberately made at the time of obtaining the photocopy of document without

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damaging the original document. It is learned that in majority of the cases fabrications are made by changing/ replacing/ overwriting/ removing/ adding contents in place of authenticated content. The fabricated photocopy documents are generated to gain some short term and long term benefits unlawfully. This poses a serious threat to the system and the economics of a nation. The types of systems trusting photocopied document raise an alarm to have an expert system [1] that efficiently supports in detecting a forged photocopy document. The need of such requirement to the society has motivated us to take up research through investigating different approaches to detect fabrication in photocopy document. It is quite evident from the above discussions that the probability of fabrication is zero in the 1<sup>st</sup> photocopy obtained from the original document, where as the fabrication may be suspected in the higher order photocopy. In this direction, an attempt is made to estimate the recursive order number of the photocopy submitted. Further, based on the estimation of order number, investigations can be explored to detect the possibility of fabrication in photocopy.

Many research attempts are carried out on original documents like signature verification, detection of forged signature [2], handwriting forgery [3], printed data forgery [4], and finding authenticity of printed security documents [5]. Literature survey in this direction reveals that the above research attempts are made in the following issues: Discriminating duplicate cheques from genuine ones [5] using non-linear kernel function; Detecting counterfeit or manipulation of printed document [4] and this work is extended to classify laser and inkjet printouts; Recognition and verification of currency notes of different countries [6] using society of neural networks along with a small work addressing on fake currencies; Identification of forged handwriting [3] using wrinkles as a feature is attempted along with comparison of genuine handwriting. One of the interesting features is a measure of the variability of the handwriting on a small scale. Although one can copy the shape of another's handwriting, it is difficult to mimic the dynamic aspects, such as speed and acceleration. Because forged handwriting tends to be drawn slowly, when scanned, it might be more wiggly than the authentic handwriting. Forgery handwriting shows more wrinkliness than natural handwriting does. This wrinkliness feature can be measured using the *fractal* dimension measure.

While preparing any security document, the designers embed certain features that are considered as security features. It is generally assumed that these features are difficult to replicate or copy. Duplicity of a document is identified by checking these security features. Security features in documents like cheques, legal deeds, certificates, etc. are embedded by three attributes namely (i) color features, (ii) background artwork and logo, and (iii) paper quality. After the extracting features from a cheque document, its authentication is to be done. This is modeled as a 2-class pattern recognition problem, i.e. whether the document belongs to the genuine document class or not. Support Vector Machines(SVMs) [5] are used to verify authenticity of these cheques.

Further, in literature to the best of our knowledge no significant effort is noticed towards detecting forgery made while taking photocopy. As the domain under consideration is new for research, no standard data set is available. Hence for the purpose of experimentation sufficient numbers of sample photocopies are obtained on a RICOH AFICIO 2018D copier machine to generate different recursive order copies. The photocopies were scanned using a scanner to produce bitmap images at 300dpi. Fig 1a and 1b show the samples of 1<sup>st</sup> order and 5<sup>th</sup> order recursive photocopies of a document respectively.

With Prime Minister Manmohan Singh maintaining that the government is open to dialogue, Anna Hazare on Monday suggested that he should send his representatives for discussion on the JanLokpalBill. Kiran Bedi, one of the leading members of Team Anna, quoted Hazare as saying, "Let the government come forward to discuss the Jan Lokpal bill. Let the PM send his representatives." She also ruled out that any negotiations were on between the two groups. "(Talk of)anynegotiationsarerumours, "Beditweeted. The suggestion came within hours of the Prime Minister saying that the government is open to a "reasoned debate" on the Lokpal Bill and that the Parliamentarypanelexaminingitcanproposechanges. "We are open to a reasoned debate on all

Fig 1a: 1<sup>st</sup> order photocopy

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Fig 1b: 5<sup>th</sup> order photocopy

Visual analysis performed on the recursive photocopied documents exhibits a relative degradation in the texture of the document. The degradation keeps relatively increasing on each recursive photocopy i.e., more the order of recursion, higher is the degradation in texture which is quite clear from fig 1a and 1b. This directed us to explore a texture analysis method to study the relative degradation in the recursive photocopies of documents. Earlier, two methods were proposed to find texture degradation. The first method uses Geometric Moments [7] to find texture degradation and the second method was proposed using entropy from Gray Level Co-occurrence Matrix [8]. The first approach showed an efficiency of 65%. In order to achieve higher efficiency exploration of another method was attempted on this problem to analyze texture degradation using probability distributions.

The remainder of the paper is organized as follows:. Section 2 gives introduction to Probability distributions used in the methods. Section 3 describes methodology adopted for estimation of order number of photocopy using texture feature. The experiments conducted along with analysis of results are discussed in section 4. Conclusion on the work is presented in section 5.

# 2. PROBABILITY DISTRIBUTIONS

In the proposed system, the recursive order of the photocopy documents is estimated based on measure of texture degradation using different distribution methodologies like Normal distribution, Exponential distribution and Extreme value distribution. These distribution methods are applied to maximum peak values which are extracted from the distribution graphs and brief introduction to the same is given subsequently.

## 2.1 Normal distribution

In probability theory, the normal (or Gaussian) distribution is a very commonly occurring distribution function that tells the probability that an observation in some context will fall between any two real numbers. Normal distributions are extremely important in statistics and are often used in the natural and social sciences for real-valued random variables whose distributions are not known [9].

The Gaussian distribution is sometimes informally called the bell curve. However, many other distributions are bell-shaped (such as Cauchy's, Student's, and logistic). The terms Gaussian function and Gaussian bell curve are also ambiguous because they sometimes refer to multiples of the normal distribution that cannot be directly interpreted in terms of probabilities [10].

A normal distribution is,

$$f(x, \mu\sigma) = \frac{1}{\sigma\sqrt{2\pi}} e^{-\frac{(x-\mu)^2}{2\sigma^2}}$$
 (1)

The parameter  $\mu$  in this definition is the *mean* or *expectation* of the distribution (and also its median and mode). The parameter  $\sigma$  is its standard deviation; its variance is therefore  $\sigma^2$ . A random variable with a Gaussian distribution is said to be normally distributed and is called a normal deviate. If  $\mu = 0$  and  $\sigma = 1$ , the distribution is called the standard normal distribution or the unit normal distribution, and a random variable with that distribution is a standard normal deviate[9].

### 2.2 Extreme value Distribution

The extreme value distribution has two forms. One is based on the smallest extreme and the other is based on the largest extreme. These are the minimum and maximum cases, respectively. The extreme value distribution is also referred o as the Gumble distribution [11]. The general formula for the probability density function of the Gumbel (minimum) distribution is

$$f(x) = \frac{1}{\beta} e^{\frac{x-\mu}{\beta}} e^{-e^{\frac{x-\mu}{\beta}}}$$
 (2)

Where  $\mu$  is the location parameter and  $\beta$  is the scale parameter. The case where  $\mu = 0$  and  $\beta = 1$  is called the standard Gumbel distribution [11]. The equation for the standard Gumbel distribution (minimum) reduces to

$$f(x) = e^{-x}e^{-e^x}$$
 (3)

# 2.3 Exponential Distribution

The exponential distribution is the probability distribution that describes the time between events in a Poisson process, i.e. a process in which events occur continuously and independently at a

constant average rate. It is the continuous analogue of the geometric distribution, and it has the key property of being memory less. In addition to being used for the analysis of Poisson processes, it is found in various other contexts [12].

The probability density function (pdf) of an exponential distribution is

$$f(x:\lambda) = \begin{cases} \lambda e^{-\lambda x} & x > 0\\ 0 & x < 0 \end{cases}$$
 (4)

Alternatively, this can be defined using the Heaviside step function [13], H(x).

$$f(x; \lambda) = \lambda e^{-\lambda x} H(x)$$
 (5)

Here  $\lambda > 0$  is the parameter of the distribution, often called the rate parameter. The distribution is supported on the interval  $[0, \infty]$ . If a random variable X has this distribution, we write  $X \sim \text{Exp}(\lambda)$ . The exponential distribution exhibits infinite divisibility [14].

Mean and standard deviation are the essentials to apply probability distribution to the images. The mean is the average of the numbers and mean is used to calculate the central value of a set of numbers [15]. The mean is denoted by the symbol ' $\overline{X}$ '. The formula for mean is,

$$\overline{X} = \frac{\sum_{i=1}^{n} x_i}{n} \tag{6}$$

Standard deviation is the measure of how the numbers are spread out. The standard deviation is denoted by the symbol ' $\sigma$ '. The formula for standard deviation is,

$$\sigma = \sqrt{\frac{1}{N}} \sum_{i=1}^{N} (x_i - \mu)^2$$
 (7)

Probability distribution function are applied to several set of samples and get a range of values through which we can predict the recursive order of the given photocopy documents

# 3. METHODOLOGY

Recursive order number is the order number of photocopy which is obtained recursively. Texture degradation is one of the noticeable feature of the recursive photocopy document. Degradation of text increases as the recursive order number of the photocopy document increases. From the Fig 1b, it is evident that degradation in the recursive photocopy is maximum on right side of the document. The work focus on measuring texture degradation only on the right edge part of the recursive photocopy. In order to estimate the recursive order of the photocopy document, different distribution functions are applied to the given photocopy document and based on the values obtained by these functions, the order of the photocopy document is estimated. In the proposed work three different distribution functions Exponential, Normal and Extreme value distributions are computed. These distribution functions are applied to the training samples, range of values for every distribution function are generated and tabulated as shown in table 1.

	Order Number							
Distribution Functions	1 <sup>st</sup>	Overlapping between 1st & 2nd	2 <sup>nd</sup>	3 <sup>rd</sup>	4 <sup>th</sup>	5 <sup>th</sup>		
Exponential	0.0211	0.0258	0.0258	0.0208	0.0189	0.0165		
	-	-	-	-	-	_		
	0.0257	0.0308	0.0308	0.0221	0.0207	0.0188		
Extreme value	0.3401	0.3623 -	0.3995	0.2735	0.2009	0.0845		
	-	0.3994	-	-	-	-		
	0.3622		0.3400	0.3400	0.2734	0.2008		
Normal	0.2107	0.2385 -	0.2567	0.1126	0.0801	0.0230		
	-	0.2566	-	-	-	-		
	0.2384		0.2886	0.2106	0.1125	0.0802		

Table 1: Range of distribution functions

From the table 1 it is noticeable that there are considerable overlapping values for order numbers one and two. This is because the texture degradation is quite narrow in these two recursive orders where as other order number classification has distinct range values. Hence, a decision system is required to make the classification in case of overlap to resolve the conflicts. Fig 2 shows the flow while making the decision.

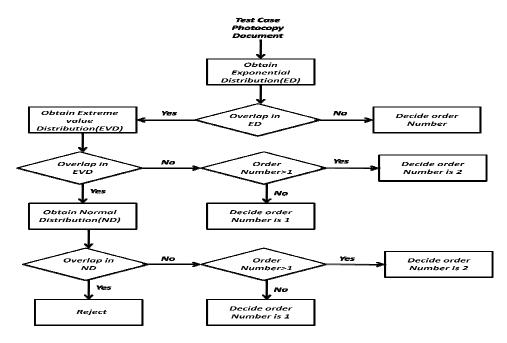


Fig2: Flow Diagram for Decision making in the proposed method

The photocopy document under consideration is subjected to obtain Exponential distribution.

The order number of the photocopy is decided if the Exponential distribution value falls within the classified range of values. In case the value is in overlap range then the Extreme value distribution is obtained. The order number is decided as 2 if the Extreme value distribution value

is in any of the range 2 or higher. The order number is decided as 1 if the value clearly falls in range of copy 1. In case of Extreme value distribution value also falls in overlap range, then Normal distribution is computed. The order number is decided as in Extreme value distribution and considered as rejection case if the value falls in the overlap range.

# 4. EXPERIMENTAL RESULTS

Experimentation is performed through testing the proposed method using synthetically generated samples of photocopy documents from different photocopying machines. Testing is carried out with sufficient number of test samples up to 5<sup>th</sup> order since higher order copies are not suitable for fabrication. The test samples include different sizes, different contents, figures, tables etc. The results of the testing are tabulated in table 2. The experiments conducted using test samples show an average classification efficiency of 83.5% with the misclassification of 11.5% and rejection is 5%. The misclassifications are mainly due to the presence of noise and dirt in the document, toner quality and machine's quality used in production of photocopies.

Order Number	No. of samples	Correct	Incorrect	Rejection	Efficiency
1 <sup>st</sup>	45	40	03	02	88.8%
2 <sup>nd</sup>	54	42	09	03	77.7%
3 <sup>rd</sup>	65	50	10	05	76.9%
4 <sup>th</sup>	42	34	06	02	80.9%
5 <sup>th</sup>	55	52	02	01	94.5%
Total	261	217	30(11.5%)	13(5%)	83.5%

Table 2: Results of testing

# 5. CONCLUSION

The implemented method provides a supervised system for estimating the recursive order of photocopy submitted. The method is essentially based on the probability distribution methods. The method shows average classification efficiency close to 84%. The misclassification is due to photocopies obtained from different machines and their quality. The proposed work is design of an efficient method to estimate the recursive order of photocopy and is a base work to continue research for better efficiency through investigating methods to find rate of degradation using variations in character thickness and line orientations. The rejection case indicates the proposed model cannot resolve the conflict and suggested for physical verification. The proposed work is prerequisite to continue the research to detect the photocopy under consideration is a fabricated or not.

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